

Scheduling and QoS scheduling

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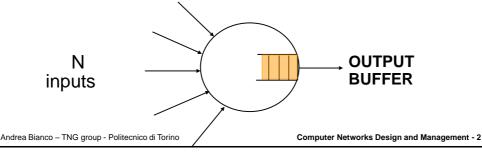
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Scheduling algorithms

- Scheduling: choose a packet to transmit over a link among all packets stored in a given buffer (multiplexing point)
- Mainly look at QoS scheduling algorithms
 - Choose the packet according to QoS needs



Output buffered architecture

- Advantage of OQ (Output Queued) architectures
 - All data immediately transferred to output buffers according to data destination
 - It is possible to run QoS scheduling algorithms independently for each output link
- In other architectures, like IQ or CIOQ switches, problems become more complex
 - Scheduling to satisfy QoS requirements and scheduling to maximize the transfer data from inputs to outputs have conflicting requirements

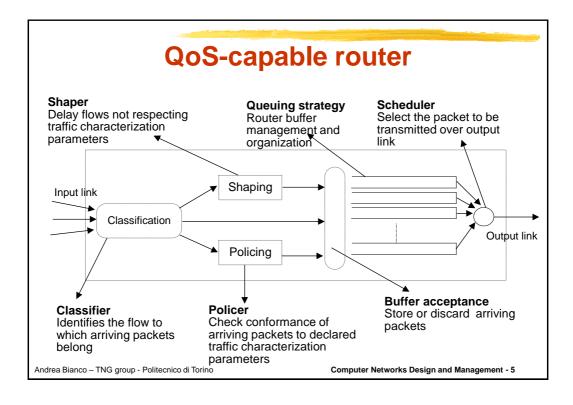
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QoS scheduling algorithms

- · Operate over multiplexing points
- Micro or nano second scale
- Easy enough to be implemented in hardware at high speed
- Regulate interactions among flows
 - Single traffic relation (1VP/1VC)
 - Group of traffic relations (more VC/1VP o more VC with similar QoS needs)
 - QoS classes
- Strictly related and dependent from buffer management techniques
- To simplify and make the problem independent, assume infinite capacity buffers
- Choice of the scheduler may have implications on CAC

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QoS scheduling algorithms: properties

- Flow isolation
 - "mis-behaving" (non conformant) flows should not damage "well-behaved" (conformant) flows
 - PER-FLOW queuing, which implies resource partitioning
 - · scheduler chooses from which queue to transmit the packet
 - Related to fairness
- · End-to-end statistical or deterministic guarantees
 - Bit rate
 - · Equal for all flows (useful for best effort traffic)
 - · Specific for each flow
 - Delay
 - Losses

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QoS scheduling algorithms classification

- · Work-conserving scheduler
 - Always transmit a packet as long as there is at least a packet available in switch buffer
 - Optimal performance in terms of throughput
- Non-work-conserving scheduler
 - May delay packet transmission
 - · No transmission even if there are packets stored in buffers
 - Reduced throughput
 - Better guarantees on delay jitter
 - · Reduced buffer size
 - In theory appealing approach, not much used in practice

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Scheduling discipline property

- Theorem
 - The sum of mean queuing delays received by a set of multiplexed connections, weighted by their share of the link load is independent of the scheduling algorithm
- A scheduling algorithm can reduce a connection mean delay only at the expense of increasing the delay of another connection
- A work-conserving scheduler can only reallocate delays among connections
- A non work-conserving scheduler can only provide a mean queuing delay larger than a work conserving discipline

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Work conserving versus non-work conserving schedulers

- Work-conserving schedulers disadvantage
 - Multiplexing point increase traffic burstiness
 - This increase packet jitter and buffering requirments to prevent losses
 - Patological scenarios demonstrate that this phenomena may become worse when the number of crossed nodes increases
- Non work-conserving schedulers have buffering requirements independent of the network depth

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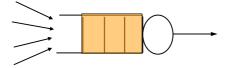
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Scheduling algorithms goals

- Best-effort traffic scheduler
 - All active flows should obtain the same amount of service
 - Possibly max-min fair
 - No delay guarantees
 - FIFO, PS (Processor Sharing), RR (Round Robin), DRR (Deficit Round Robin)
- QoS scheduler, i.e. scheduler for traffic with QoS requirements
 - Specific bit rate guarantees for each flow
 - Specific delay guarantees for each flow
- Strict priority, GPS (Generalized Processor Sharing), WRR (Weighted Round Robin), WFQ (Weighted Fair Queuing), EDD (Earliest Due Date)
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FIFO

- FIFO (First In First Out) service discipline
 - Also known as FCFS (First Came First Served)
- Single queue
- Data queued according to arrival time and served in order



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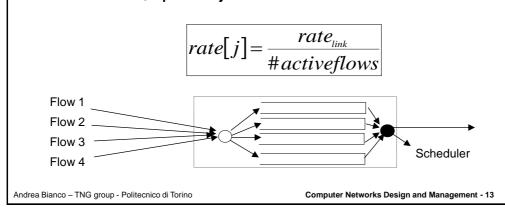
FIFO: properties

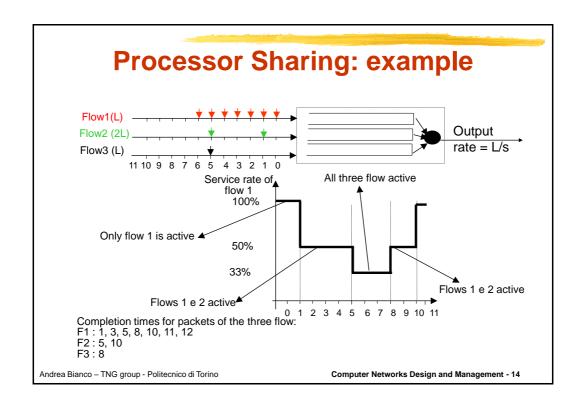
- · Work-conserving
- Complete sharing of link bit rate and buffer space: no protection against non conformant flows
- · All flows observe similar delay performance
 - Suited to best-effort traffic
- Neither bit rate (bandwidth) guarantees nor loss guarantees
 - Performance depend on the amount of ingress data traffic of each flow
- Aggressive flows obtain better performance
 - Unfair

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Processor Sharing

- · Ideal work-conserving scheduler for best effort
- Each queue served according to a fluid model
- · At time t, queue j is served at rate





Processor Sharing

Pros

- If no data are discarded, a network of PS schedulers provides rates close to a max-min fair allocation
 - Rate of the max-min allocation only downstream from the bottleneck link
 - · Fairness does not require congestion control mechanisms
 - · If dropping packets, fair dropping must be ensured

Cons

- Ideal solution, non practical (packets are not fluids)
 - · Devise approximations

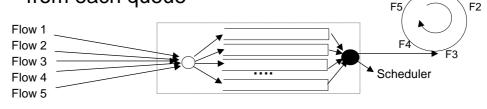
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Round Robin

- Processor sharing approximation
- Buffer organized in separate queues, one queue for each active flow
 - Each queue is a FIFO queue

 Service cycle among queues, one packet from each queue



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Round Robin

- May have some delay bias
- To improve delay fairness, at each serving cycle it is possible to modify queue service order
 - At time 0, queue service order: 1,2,3,..,K
 - At time 1, queue service order: 2,3,..,K,1

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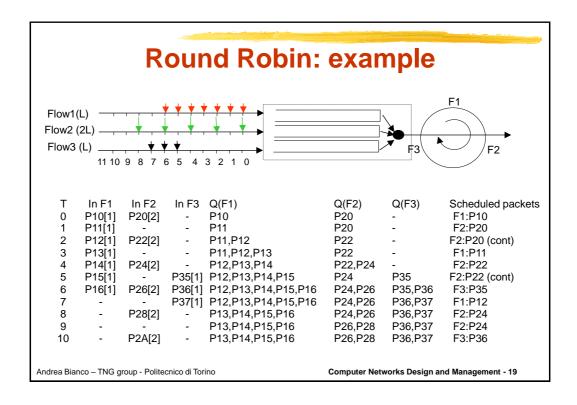
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Round Robin: properties

- Relatively easy to implement in hardware
- Guarantees flow isolation
 - Through queue separation
- · Service rate of each queue:
 - C/K, for fixed packet size and k flows
 - For variable packet size, some rate unfairness may arise (fair in #packets per flow)
 - Taking into account packet size makes implementation more complex

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Scheduling in OQ architectures



Deficit Round Robin

- Round robin work conserving scheduler working with variable packet size
- One queue[i] per flow i
- The scheduler visits each queue in a round robin fashion
 - Each queue[i] has a deficit counter D[i] associated with
 - F[i] is increased by a fixed quantum when queue[i] is visited
 - Send the packet if D[i] large enough wrt packet size

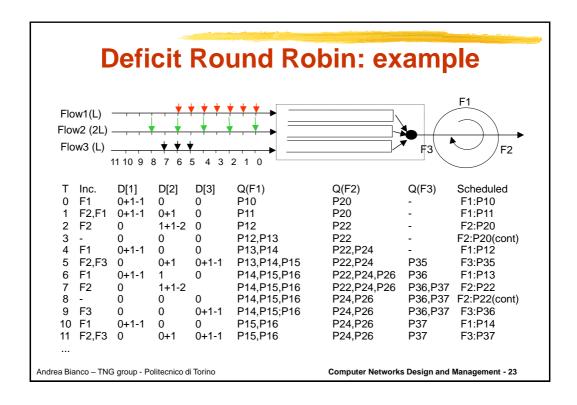
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DRR: pseudo code

Deficit Round Robin

```
if (length_first_packet of queue[i] > d[i])
{ packet is kept in queue[i] }
else
{packet transmitted on output link;
d[i]=d[i]- packet_length;
if (queue [i] is empty) { d[i]=0; }
```

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Deficit Round Robin

- The idea is to keep track of queues that were not served in a round (compute deficit) and to compensate in the next round
- Keep an active list of indices of queues that contain at least a packet to avoid examining empty queues
- May be a problem to define the quantum
 - If too small, may need to visit too many times queues before serving a queue
 - If too large, some short term unfairness may arise
- Fair only over a time scale longer than a round time
 - Round time is a function of the number of flows and packet size
 - At a shorter time scale, some flows may get more service
 - Small packet size or high transmission speed reduce the round time

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Strict priority

- First attempt to define a QoS capable scheduler
- Buffer partitioned in k queues, k being the number of priority classes
- Each queue is associated with a different priority
- Data unit are stored in a queue according to their priority level
- Higher priority queue is always served. Only if empty, the lower priority is considered
 - Non preemptive service: packet under service finish transmission
- Within each queue, data are served according to a FIFO service discipline

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Strict priority algorithm

- Work-conserving
- Easy to implement
- Perfect isolation for high priority queue only, low priority queues may even suffer starvation (if CAC is not adopted on high priority queues)
 - Fair?
- · No bit rate, loss and delay guarantees
- No isolation among flows stored in the same FIFO queue, i.e., within the same priority level

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Generalized Processor Sharing

- · Fluid system used as an ideal reference
- · One queue for each flow
- Each queue is served as if it contains a fluid flow, i.e. by an infinitesimal fraction of time
- Each queue j is associated with a weight w[j], normally derived from bit rate requirements
- At time t, queue j is served at rate:

$$rate[j] = rate_{link} \frac{w[j]}{\sum_{i=active aueus} w[i]}$$

- A queue is active if it contains some fluid
- If the number of active flows decreases, excess bit rate is redistributed in proportion to queue weight
- CAC algorithms must control the rate of served flows, otherwise bit rate guarantees cannot be obtained

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GPS properties

- Work conserving with flow isolation
- Per flow bit rate guarantees
 - When using a single GPS scheduler
 - When using a network of GPS schedulers
- End-to-end delay guarantees for token bucket (r,b) constrained flows
- · Provides bounds on buffer size
- Simple jitter delay guarantees ([0,Dmax])
- Ideal scheduler, practical approximations

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GPS approximation

- Frame-based
 - Define a service cycle (frame)
 - Allocate frame portion to each flow
 - Example: WRR (Weighted-Round Robin),
 WDRR (Weighted Deficit Round Robin)
- Sorted priority
 - Compute a timestamp (tag) and associate it with each packet
 - Packets are ordered for increasing timestamp
 - Examples: Virtual Clock, WFQ (Weighted Fair Queuing), SCFQ

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WRR: Weighted Round Robin

- GPS approximation
- Buffer partitioned in N queues
 - each queue served according to a FIFO discipline
- A weight w_i ∞ requested bit rate is associated with each queue
- A service cycle among queues is executed, each queue being served proportionally to its weight, i.e., w_i per cycle
- Cycle length is the summation of the weights (possibly normalized)

$$\begin{array}{ccc}
1 & \longrightarrow & & & \\
2 & \longrightarrow & & & \\
N & \longrightarrow & & & \\
\end{array}$$

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W_N Computer Networks Design and Management - 30

WRR: Weighted Round Robin Flow 1 W₁=4 Flow 2 W₂=2 Flow 3 W₃=1 Scheduler Flow 4 W₄=1 Flow 5 W₅=1 If all flows are active

- - F1 obtains 4/9 of the link bit rate
 - F2 obtains 2/9
 - F3, F4 and F5 obtain 1/9

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WRR: properties

- Work-conserving
- · Flow isolation guaranteed
- For each queue i:
 - bit-rate = $w_i / (\Sigma_i w_i) link_rate$
 - · if all packets are of the same size
- Easy to implement (for a small number of flows)
- · Define a service cycle

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WRR: problems

- · Service cycle (and fairness) may become long when
 - Many flows are active
 - Flows have very different weights
 - On a 45Mbit/s link, 500 flows with weight 1 and 500 flows with weight 10
 - Service time of one cell (48 ytes) 9.422us
 - A cycle requires 500+500*10=5500 service time=51.82ms
- · Service provided to flows may be bursty
 - Avoidable, but complex
- For each variation of the number of active flows (departure, arrival) service cycle must be redefined
 - How to deal with the remaining part of the cycle?
- To deal with variable packet size may use WDRR, Deficit Round-Robin extended to weight support
- · Note. WRR may be exploited in best effort scenario
 - May use weights in WRR to compensate for variable packet size for best effort traffic (requires knowledge of flow average packet size)

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Sorted priority approximation to GPS

- Per-flow queuing
- Data (cells) served on the basis of negotiated rate and cell arrival time
 - Each data has a tag (urgency) assigned
- Data are inserted in a Sorted Priority Queue on the basis of data tag
- Data are served according to tag ordering
- Several algorithms: virtual clock, WFQ o PGPS, SCFQ

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Virtual Clock

- Time Division Multiplexing emulation
- Each flow j has an assigned service rate r_i
- To each data k of length L_j^k belonging to flow j, a tag (label, urgency, auxiliary virtual clock) is assigned
 - Tag represents the data finishing service time (starting service time + service time) in a TDM system serving flow j at rate r_i:

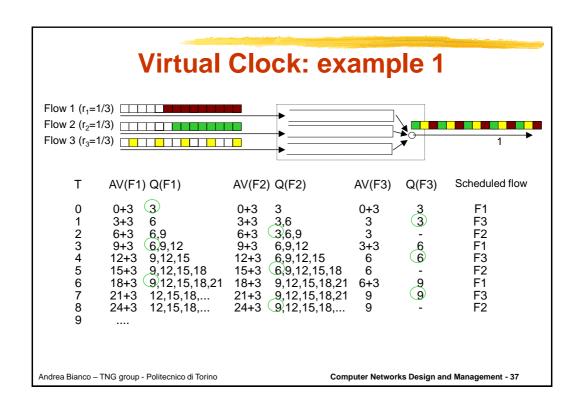
Aux
$$VC_j^k = Aux VC_j^{k-1} + \frac{L_j^k}{r_j}$$

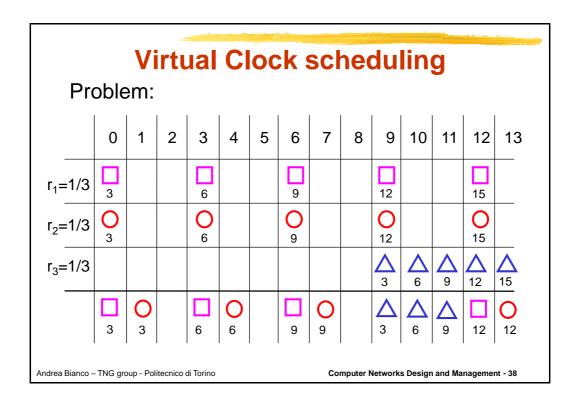
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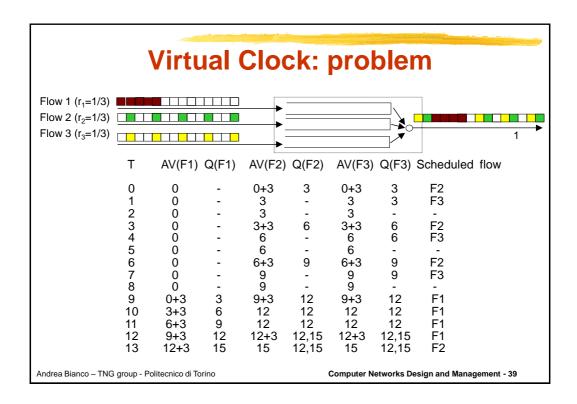
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Virtual Clock scheduling Example 2 3 5 7 4 $r_1 = 1/3$ $r_2 = 1/3$ 12 15 18 12 15 18 Service order: Andrea Bianco - TNG group - Politecnico di Torino Computer Networks Design and Management - 36

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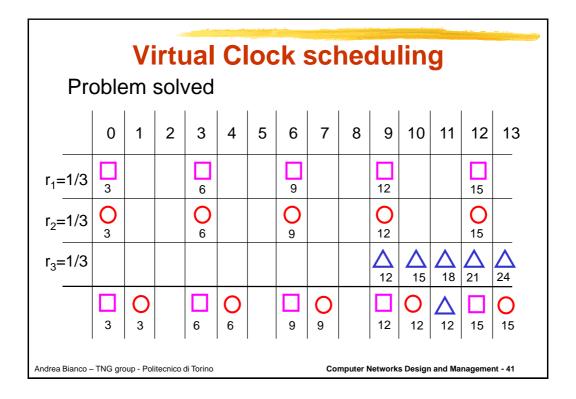
Virtual Clock

- Long term fairness with some problems
 - Inactive flows "gain time" and get more service in the future, penalizing, and even starving, other active flows (even conformant flows)
 - Clock of different flows proceed independently
- Modify the tag computation, taking into account system real time:

Aux
$$VC_j^k = \max (Aux VC_j^{k-1}, a_j^k) + \frac{L_j^k}{r_j}$$

– where a_i^k is the arrival time of cell k of flow j

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| Modified Virtual Clock Another problem | | | | | | | | | | | | | | |
|--|---|------------------|------------------|----------|-------------|-------------|---------|---------|---------|-------------|----|-------------|---------|----|
| Time | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
| r ₁ =1/3 | 3 | 6 | 9 | 12 | 15 | 18 | 21 | 24 | 27 | 30 | 33 | 36 | 39 | |
| r ₂ =1/3 | 3 | <mark>О</mark> Ф | <mark>О</mark> Ф | O | O 15 | O 18 | O 21 | O 24 | O 27 | 30 | 33 | O 36 | 39 | |
| r ₃ =1/3 | | | | | | | | | | | | | 15 | 18 |
| | 3 | 3 | 6 | O 6 | 9 | 9 | 12 | O 12 | 15 | O 15 | 18 | O 18 | <u></u> | 18 |
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Virtual Clock

- Even the modified version of Virtual clock can lead to unfairness
- Clocks of flows are now synchronized by the system time
- However, tags may overcome the system time when flows get excess bandwidth
- Excess bandwidth must be redistributed among flows to ensure work conserving property but reallocation must not penalize flows in the future

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WFQ (Weighted Fair Queueing) or PGPS (Packetized GPS)

- Algorithms that try to approximate GPS behavior
 - The minimum amount of service that can be provided cannot be smaller than the service time of a cell, since no preemption is admitted
- At time τ , the transmitted packet is the packet whose service would finish first in the GPS system if no other packets arrive after τ
 - Need to emulate the GPS system

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WFQ or PGPS

Example:

- 1 flow with negotiated rate 0.5
 - 10 fixed size packets arrive at rate 1 starting at time 1
- 10 flows with negotiated rate 0.05
 - 1 packet arrives at time 1

1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 **Time** P5 P6 P7 P8 P9 Ideal fluid P11 system GPS P20 P3 P4 P5 P6 P7 P8 P9 P10 P11 P12 P13 P14 P15 P16 P17 P18 P19 P20 WFQ service order Computer Networks Design and Management - 45

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WFQ o PGPS

- Tag computation
 - Tag should represent the finishing service time of data in the GPS system
 - However, it is fundamental to compute the tag when data unit are received at buffer input
 - Future should be known, since the data finishing service time in the ideal system depends on flow activation in the future
 - The problem is trivial if all flows are always active, since service rate are fixed

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WFQ or PGPS

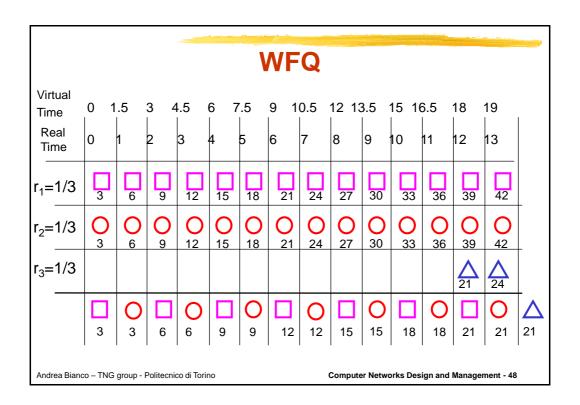
• Tag computation: $\mathcal{F}_j^k = \max \; \{ \; \mathcal{F}_j^{k\text{-}1}, \; V(a_{j^k}) \; \} + \frac{L_j^k}{\phi_i}$

 V(t) is the system virtual time or system potential (k active flows):

$$\begin{aligned} &V(0) = 0 \\ &\frac{\partial V}{\partial \tau} = \frac{1}{\Sigma_k \phi_k} \end{aligned}$$

 If flows are always active, the virtual time corresponds exactly to the real time

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WFQ o PGPS

- · Very complex to implement
- · Same properties of GPS
 - WFQ can emulate the ideal GPS system with a time difference bounded by the maximum size packet!
- Several variations were proposed
 - Indeed, in WFQ packets are never delayed too much, but could be transmitted too early
 - WF²Q
 - · improves the similarity of service order to GPS
 - among available packets, the packet with the smallest tag is chosen but only among packets whose service has already started in the ideal GPS system

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WFQ vs WF²Q 10 11 12 13 14 15 16 17 18 19 20 P5 P2 P3 P4 P6 P7 P8 P9 P10 **GPS** P11 P20 P8 P9 P10 P11 P12 P13 P14 P15 P16 P17 P18 P19 P20 WFQ service order P19 P10 P20 WF2Q service order Andrea Bianco - TNG group - Politecnico di Torino Computer Networks Design and Management - 50

SCFQ

(Self Clocked Fair Queueing)

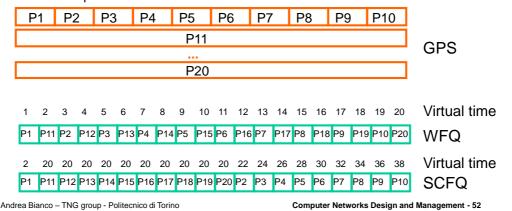
- · Variation of PGPS, simpler to implement
- · Does not require emulation of GPS system
- · Uses a simplified virtual time
 - Virtual time is set to the tag of the packet being serviced

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SCFQ vs WFQ

- 1 flow with negotiated rate 0.5
 - 10 fixed size packets arrive at rate 0.5 starting at time 0
- 10 flows with negotiated rate 0.05
 - 1 packet arrives at time 0



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Delay bounds

- · Can be computed for token bucket limited flows (R,B)
- Guarantees independent of other flow behavior
- Max delay through n scheduler (excluding fixed delays):

$$\begin{array}{ll} - \ \mathsf{GPS} & \frac{B}{R} \\ - \ \mathsf{WFQ/PGPS} & \frac{B + n \cdot P_{\max}}{R} + \sum_{i=1}^n \frac{P_{\max}}{C_i} \\ - \ \mathsf{Virtual\ Clock} & \frac{B + n \cdot P_{\max}}{R} + \sum_{i=1}^n \frac{P_{\max}}{C_i} \\ - \ \mathsf{SCFQ} & \frac{B + n \cdot P_{\max}}{R} + \sum_{i=1}^n \frac{k_i \cdot P_{\max}}{C_i} \end{array} \quad \begin{array}{ll} \bullet \ \mathsf{C_i} \ \mathsf{output\ rate} \\ \bullet \ \mathsf{k_i} \ \mathsf{number\ of\ flows} \\ \bullet \ \mathsf{P}_{\max} \ \mathsf{maximum\ packet\ size} \end{array}$$

· Bandwidth delay coupling

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EDD (Earliest Due Date)

- In classical EDD
 - Each packet is assigned a deadline
 - Packets served in deadline order
 - Deadline satisfied only if the scheduler is not overcommitted
- Traffic divided in classes
 - Each class i is characterized by a service deadline d_i
- Scheduler selects, at time t, the packet with the smallest residual time
 - Each packet is time stamped with time t_k on arrival
 - Residual time of a packet = $t_k + d_i t$
 - the amount of time left before packet service deadline expires
- EDD tends to equalize the probability of violating the delay constraint

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EDD (Earliest Due Date)

- Need to specify the process to assign deadlines
 - Delay EDD and Jitter EDD
- Delay EDD
 - packets belonging to sources obeying a peak rate constraint are assigned a worst case delay (in each node, deadline=expected arrival time+delay bound)
 - CAC must run a schedulability test to check if deadlines can be satisfied
 - Delay bound independent of bandwidth constraint (but need to reserve the peak)
- Jitter EDD
 - Delay jitter regulator in front of a EDD scheduler (non work conserving, see later)
- Issues
 - Interesting to manage delays, difficult to deal with bandwidth guarantees
 - Complex to implement (timers, dealing with real numbers)

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Non work-conserving algorithms

- Packets can be scheduled only if eligible
- · Eligibility through traffic regulators
 - Rate-jitter regulator
 - · Bounds maximum rate
 - Delay jitter regulator
 - · Compensates for variable delay at previous hop
- After the regulator use a scheduler (may be FIFO)
- Properties
 - Reduced throughput
 - Worse average delays but
 - · Control on delay jitter
 - · Reduced buffer size
- Examples
 - Stop and go
 - Hierarchical round robin

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Regulators for non work-conserving algorithms

- Rate jitter regulators
 - E.g.: peak rate regulator
 - eligibility time of a packet is the eligibility time of the previous packet plus the inverse of the peak rate (time taken to serve the packet at the peak rate)
- Delay jitter regulators
 - The sum of the queuing delay in the previous switch and the regulator delay is constant
 - · Eliminates the delay variability induced by the queuing delay at the previous hop
 - The output stream is a time shifted version of the traffic at input
 - · Time shift equal to propagation delay plus delay bound (worst case) at previous switch
 - Burstiness cannot build up
 - Do not protect against misbehaving sources
 - Very complex to implement (it requires clock synchronization)
- Note: by properly selecting the regulator and the scheduler a wide range of work-conserving and non work-conserving schedulers may be emulated
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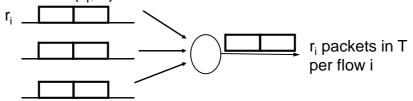
An example of a non workconserving scheduler: Stop & go

- Framing strategy
 - Time axis divided into frames of length T
- At each switch, the arriving frame of each incoming link is mapped to the departing frame of the output link by a constant delay smaller than T
- Transmission of packets arriving on any link during a frame are postponed to the beginning of the next frame

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Stop & go

- Packets on the same frame at the source stay in the same frame throughout the network
- If the traffic is (r_i,T) smooth at source i, it will remain (r_i,T) smooth



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Stop & go

- As long as each node can ensure local delay bound, end-to-end delay bound can be guaranteed
- Problem of coupling between delay bounds and bandwidth allocations granularity
 - Assume a fixed packet size P
 - Minimum bandwidth can be P/T
 - Delay bounded by two time frames T
 - Reducing T, reduced the delay but increases the minimum bandwidth
- · Generalized stop&go with multiple frame sizes
 - Coupling still exist, but can have low delays for some flows and fine bandwidth granularity for other flows

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Scheduling in OQ architectures

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